

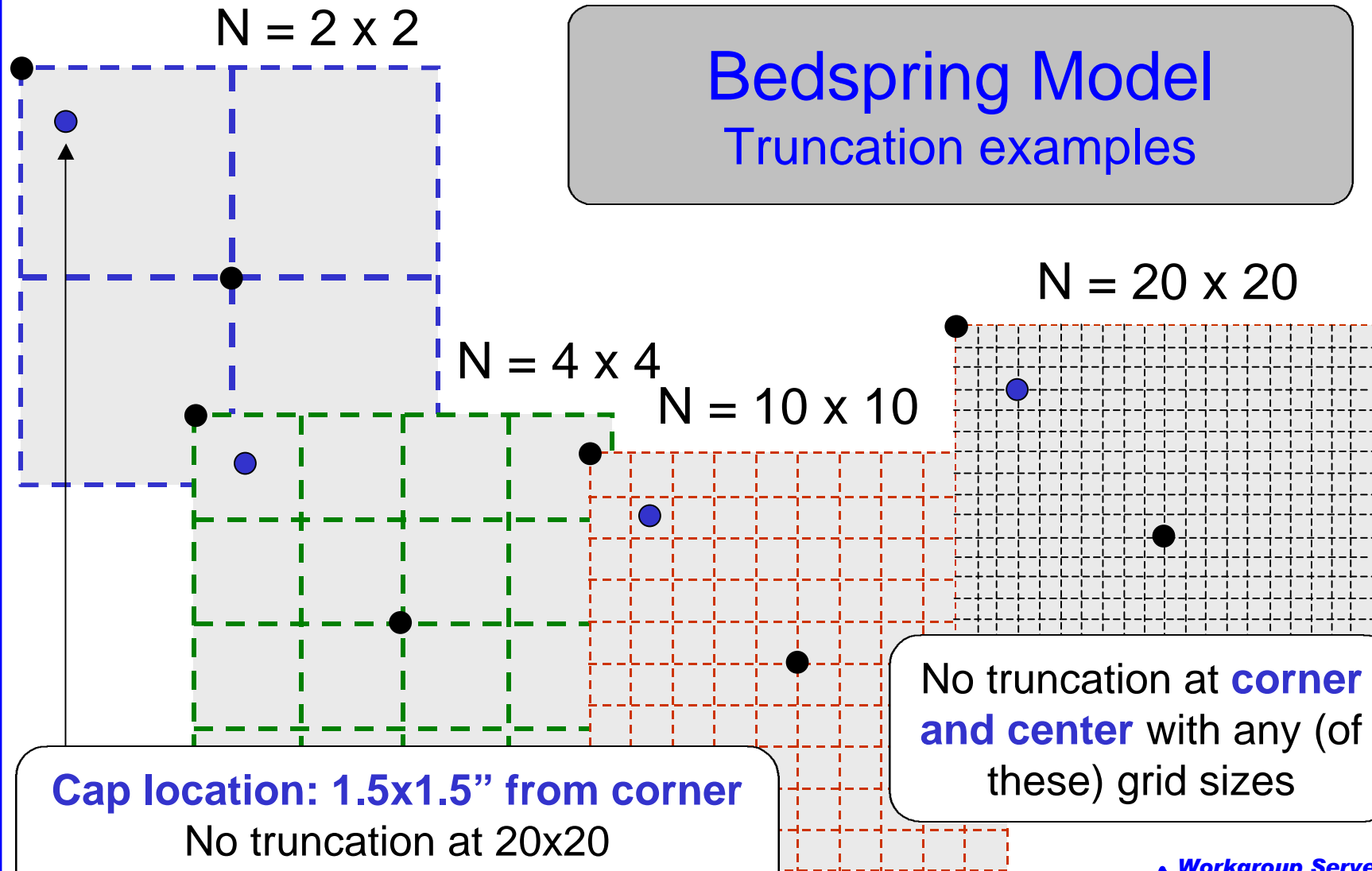
Accuracy Considerations of Power-Ground Plane Models

Outline

- Bedspring model truncation limitations
- Analytical model summation-limits
- Measured-simulated plane-bandwidth correlation
- Conclusions

Bedspring Model

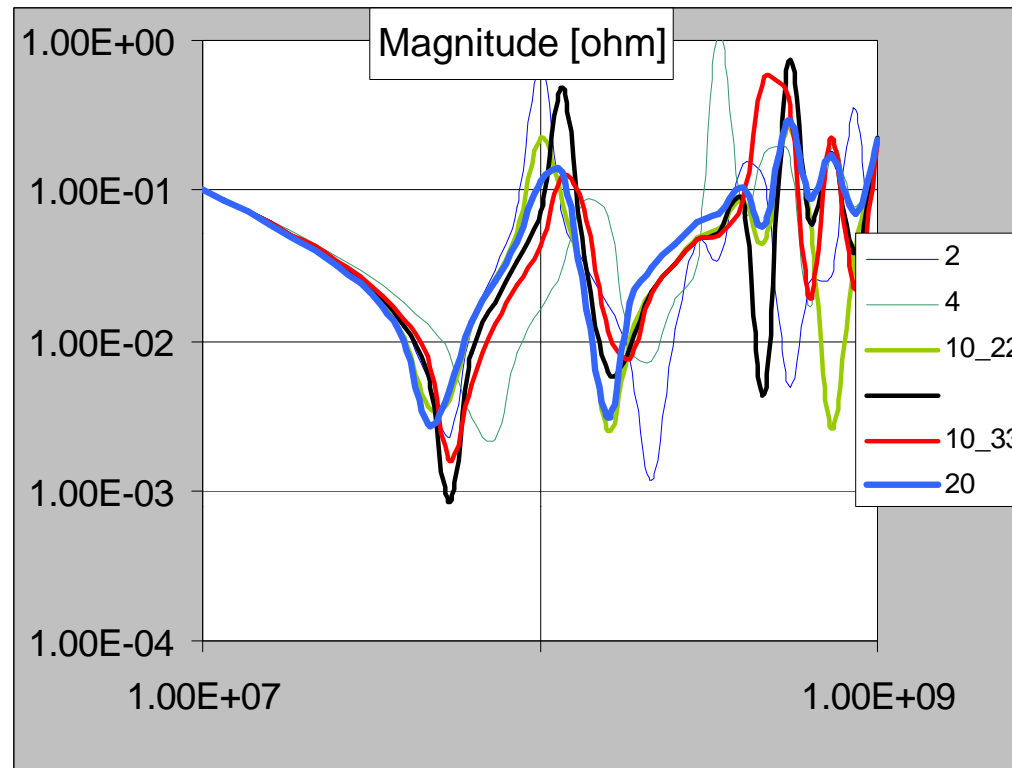
Truncation examples



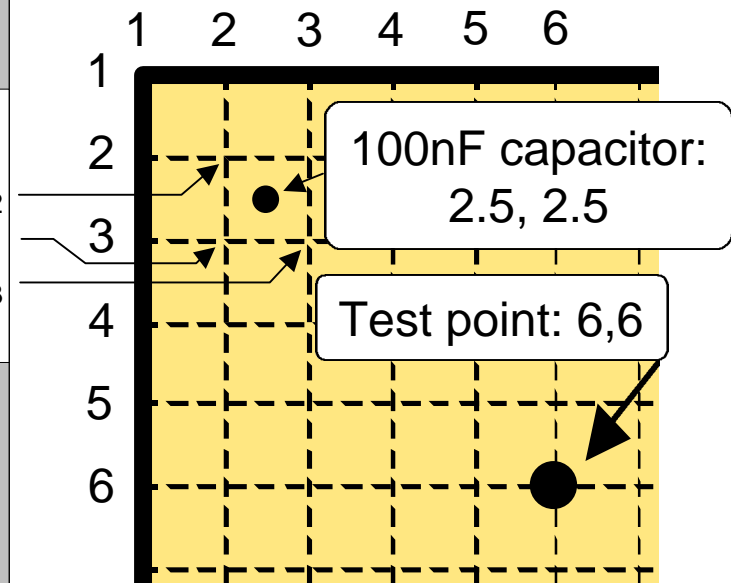
Bedspring Model Limitations

- Finite granularity of the equivalent circuit. The accuracy of model gradually decreases at frequencies where the delay through one segment of the circuit becomes a non-negligible fraction of the period of signal.
- Truncation of component and test locations. The simple bedspring model has a uniform grid step along one or both axes. If transient sources, bypass capacitors or probe points are located off grid, their locations should be truncated/adjusted to the nearest grid point.

Self-Z at Middle, One Capacitor



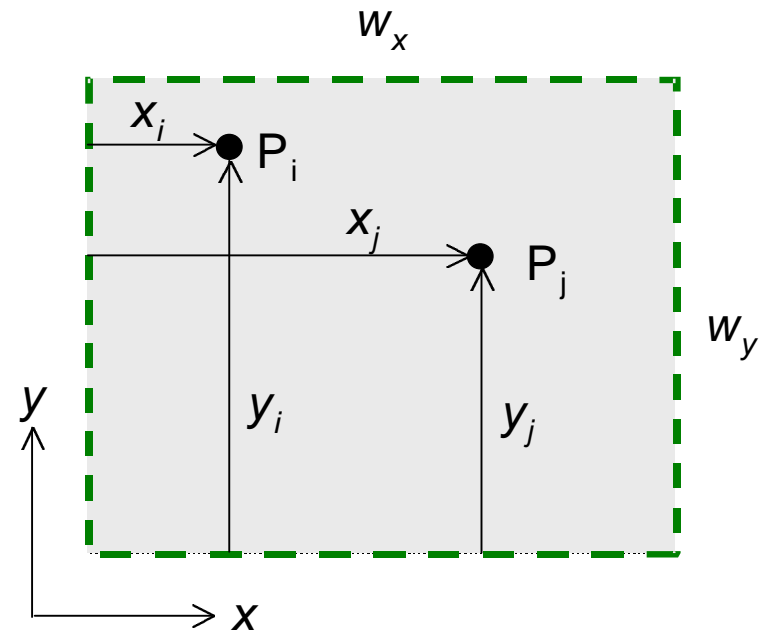
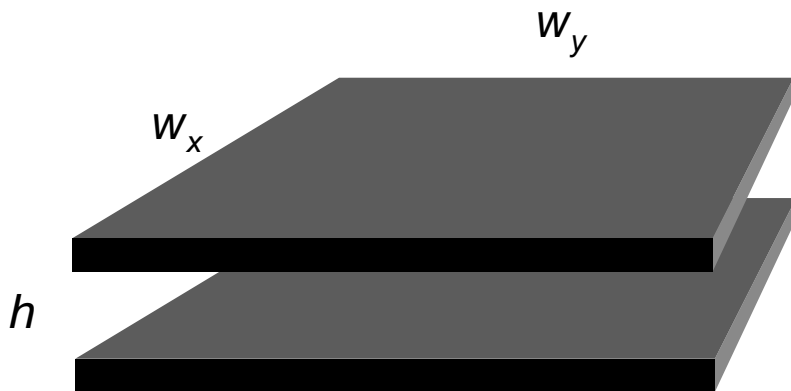
10"x10"x0.002"
One 100nF capacitor at
1.5"x1.5" from corner
No truncation at test point
Truncation for cap location



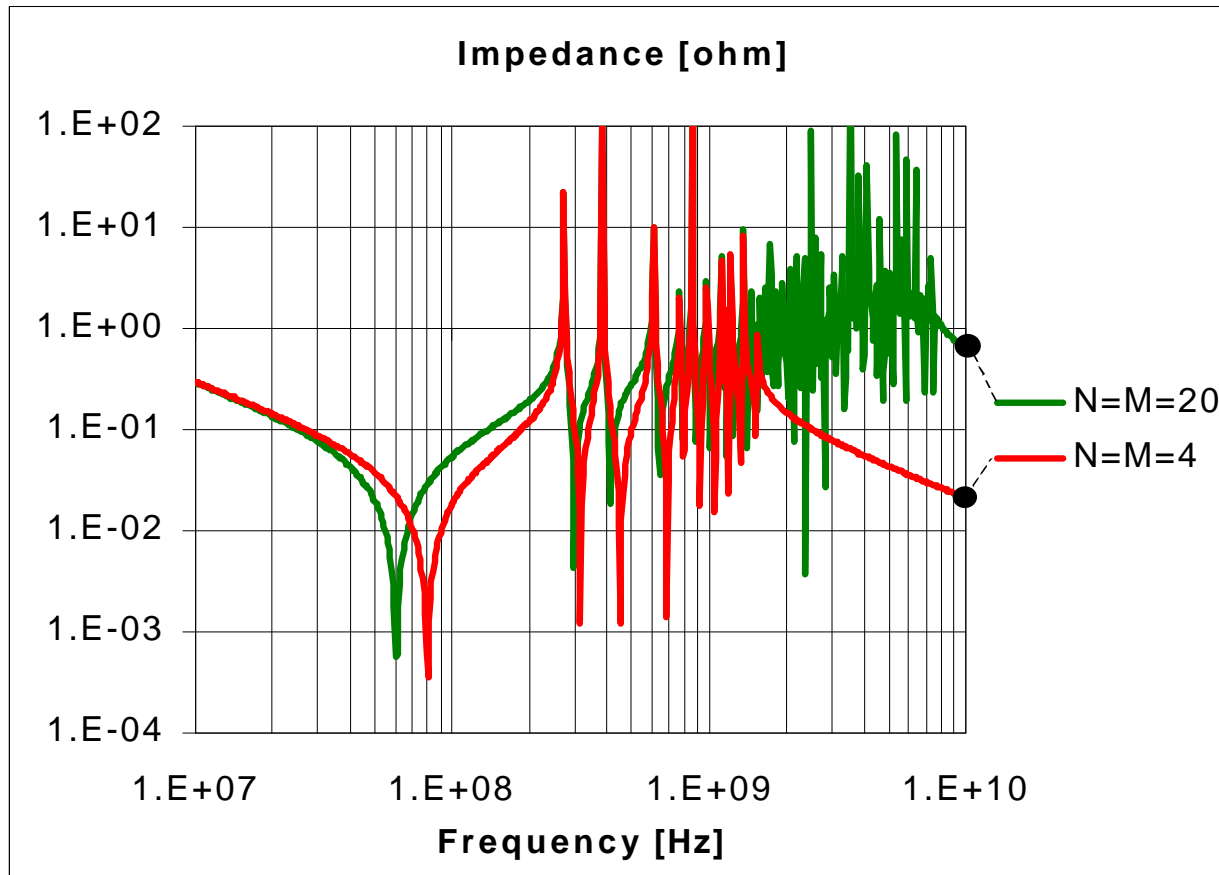
Analytical Model

$$Z_{ij}(\mathbf{w}) = j\mathbf{w}\mathbf{m}h \sum_{n=0}^{\infty} \sum_{m=0}^{\infty} \frac{c_{mn}^2}{w_x w_y (k_n^2 - k^2)} \cos\left(\frac{2m\mathbf{p} x_i}{2w_x}\right) \cos\left(\frac{2n\mathbf{p} y_i}{2w_y}\right) \cos\left(\frac{2m\mathbf{p} x_j}{2w_x}\right) \cos\left(\frac{2n\mathbf{p} y_j}{2w_y}\right)$$

Double series of
second-order
poles

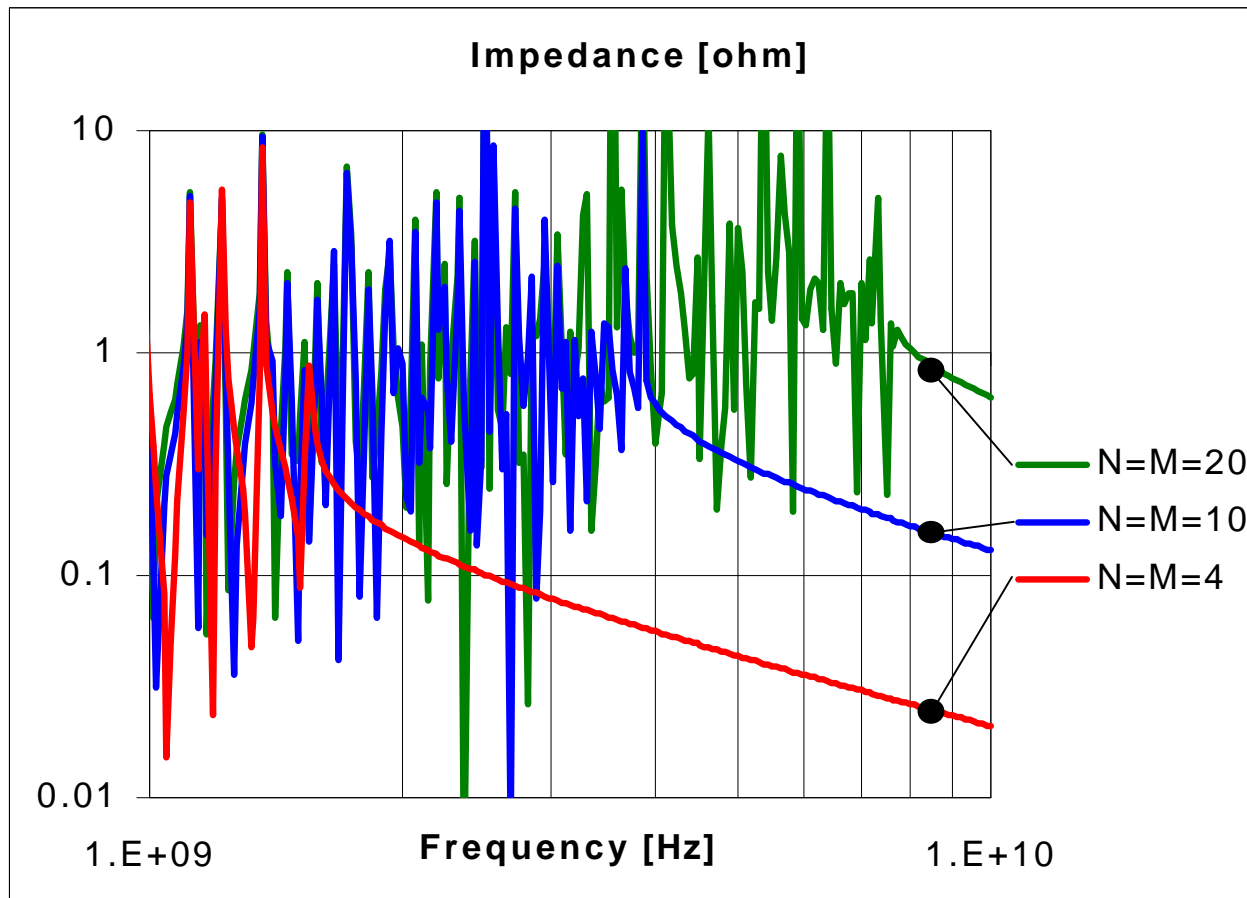


Analytical Model, Overall View



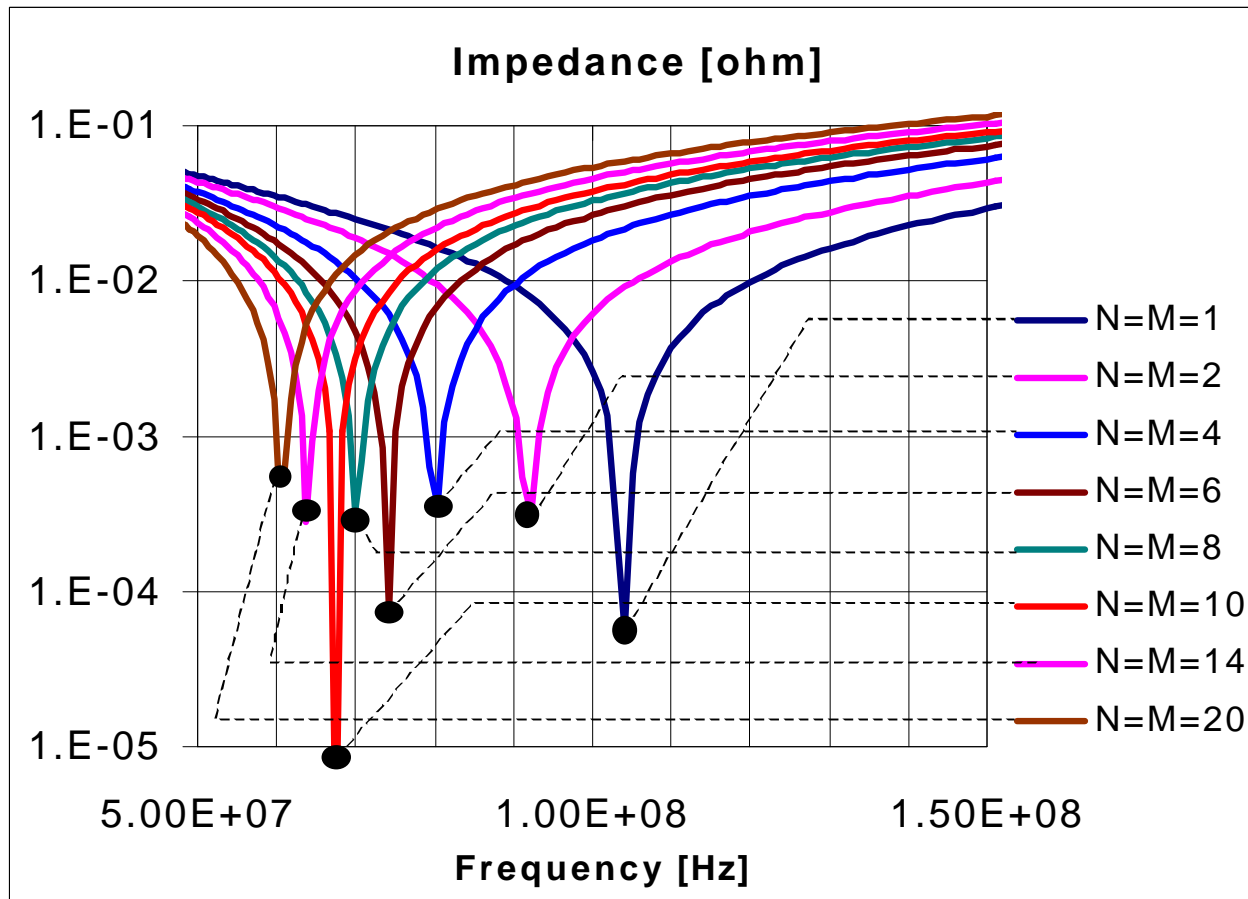
Impedance plot details depend on summation limits
(10"x10"x0.002"
FR4, self-Z at corner)

Analytical Model, High-Frequency



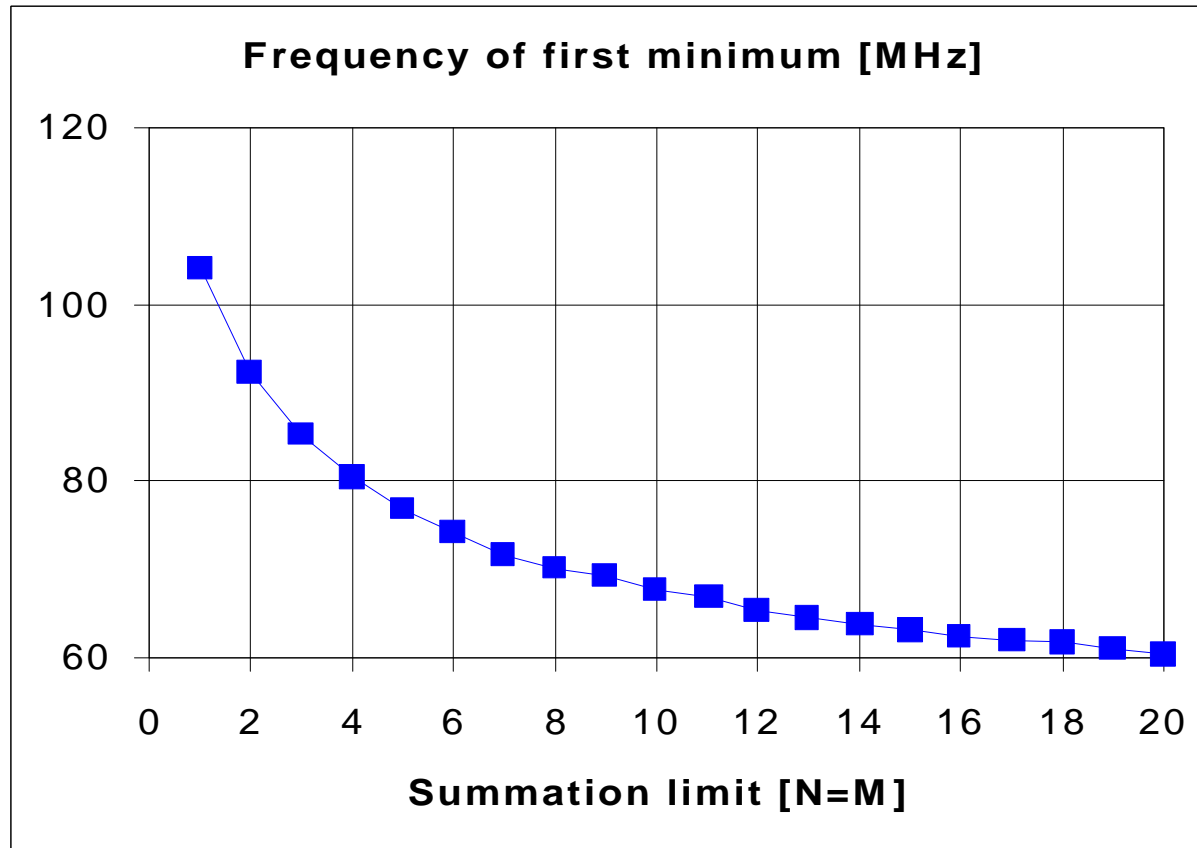
At high frequencies, Z falls beyond the last summation peak (10"x10"x0.002" FR4, self- Z at corner)

Analytical Model, Minima



At low frequencies, minima depend on summation limits (10"x10"x0.002" FR4, self-Z at corner)

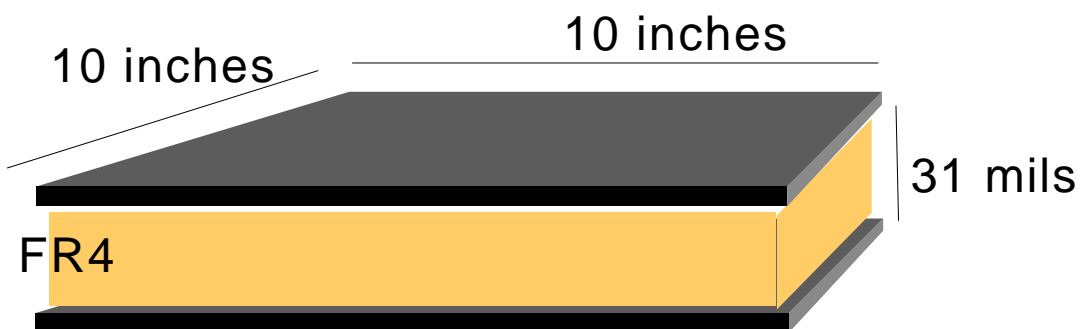
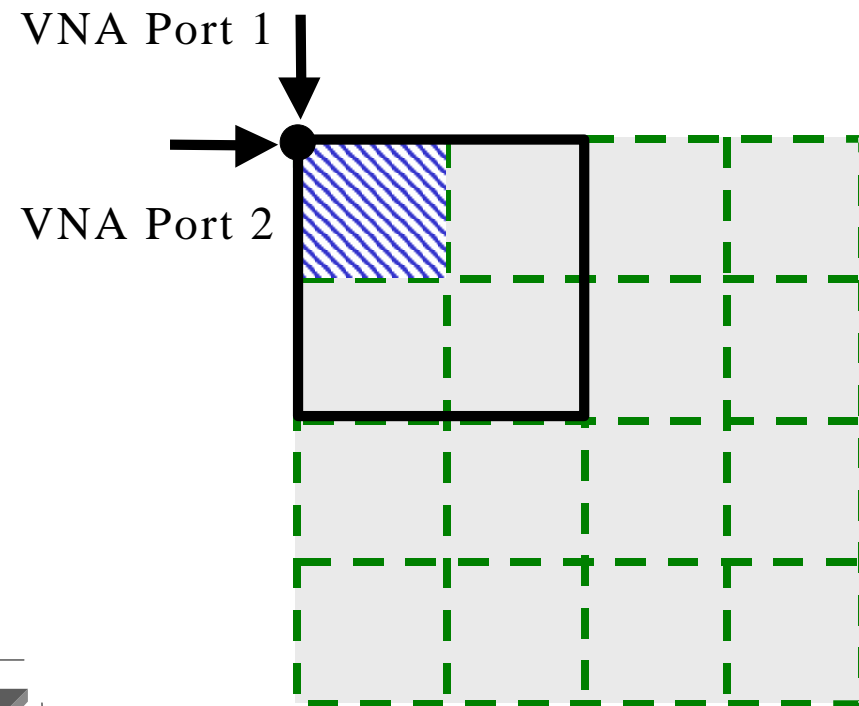
Shift of First Minimum



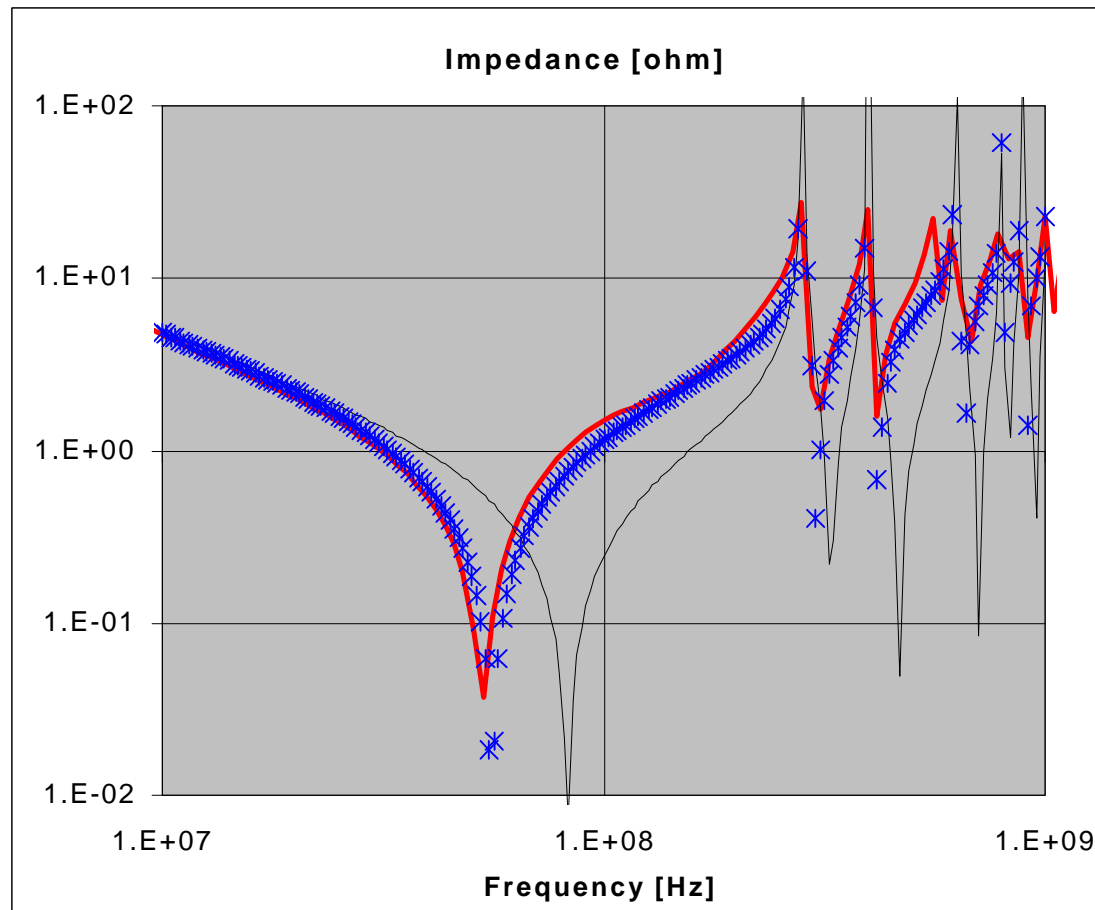
10"x10"x0.002"
FR4, self-Z at
corner

Plane Bandwidth Test Setup

- Two-port VNA impedance measurement setup
- Test point (self Z) unchanged at corner
- Plane size is cut x2, x4

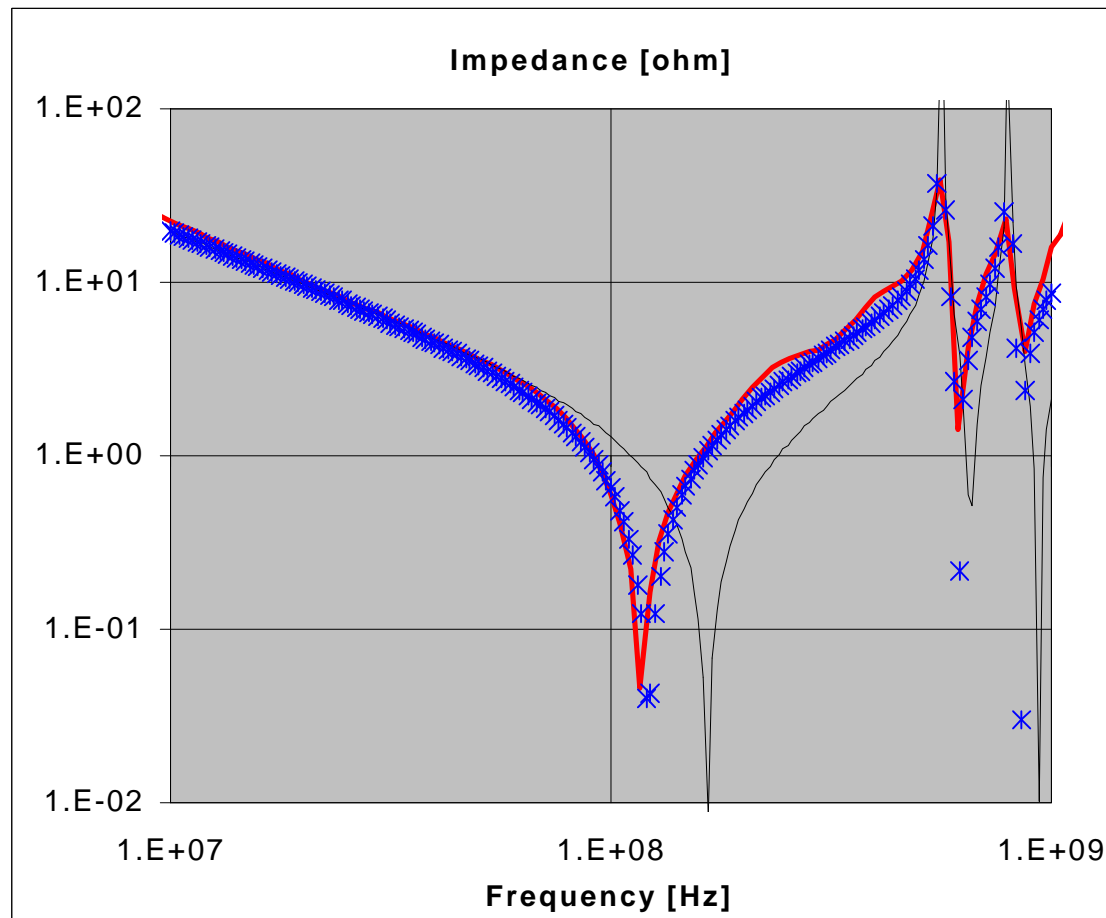


Bandwidth Test, Full (10"x10") Size



Heavy solid:
measured
Crosses:
analytical with
 $N=M=50$
($f_c \sim 10\text{GHz}$)
Thin solid:
analytical with
 $N=M=4$

Bandwidth Test, Half (5"x5") Size

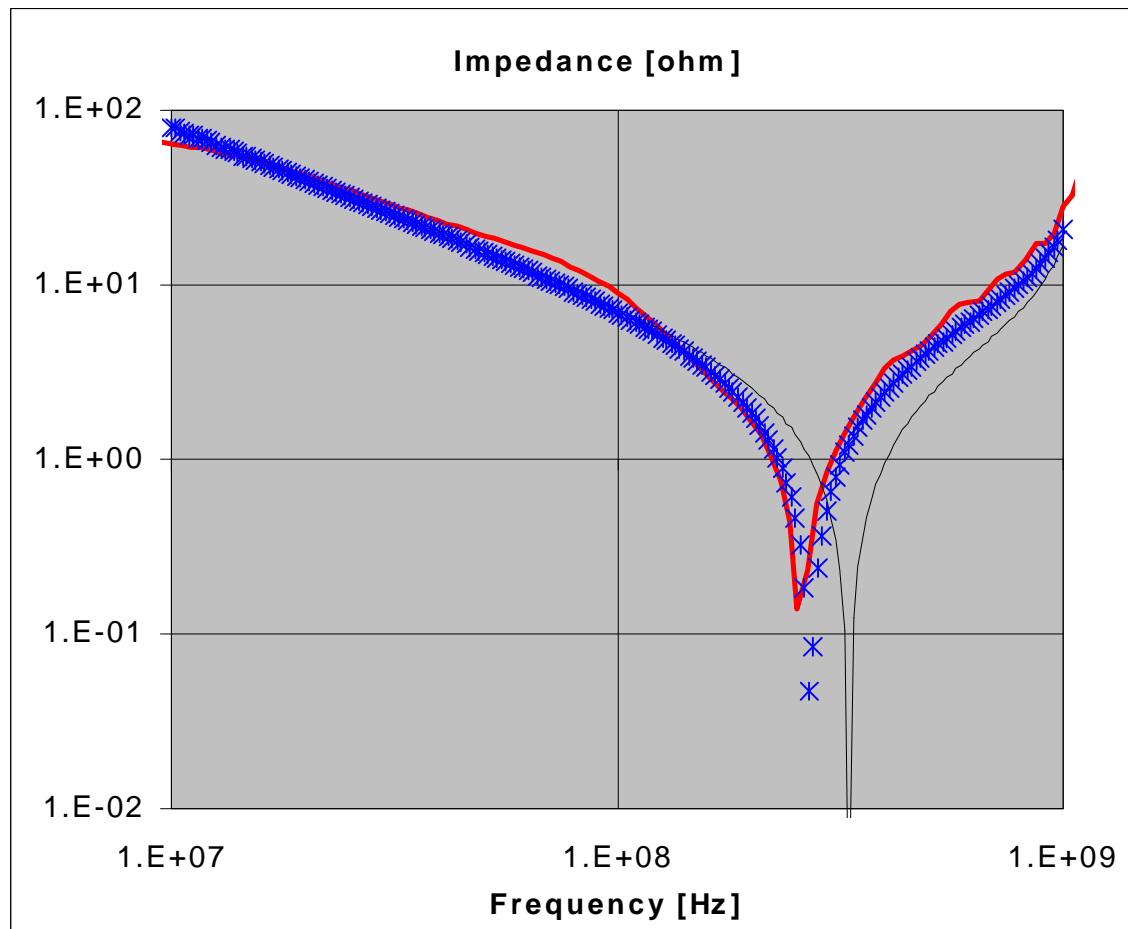


Heavy solid:
measured

Crosses:
analytical with
 $N=M=25$
($f_c \sim 10\text{GHz}$)

Thin solid:
analytical with
 $N=M=4$

Bandwidth Test, Quarter (2.5"x2.5") Size



Heavy solid:
measured

Crosses:
analytical with
 $N=M=12$
($f_c \sim 10\text{GHz}$)

Thin solid:
analytical with
 $N=M=4$

Conclusions

- Bedspring plane models exhibit quantization limitations in space
- Analytical models exhibit quantization limitation in frequency domain
- Bandwidth of plane pairs:
 - Strong function of material and plane separation
 - Weak function of plane dimensions
- Analytical model summation limits should match bandwidth of planes